

East Los Angeles College
Department of Mathematics
Math 115

Test 2

Solutions

Solve for the indicated variable.

1) $d = rt$ for r

$$\frac{d}{t} = \frac{rt}{t}$$

$$\frac{d}{t} = r \quad ; \quad \boxed{r = \frac{d}{t}}$$

✓

2) $C = 2\pi r$ for r

$$\frac{C}{2\pi} = \frac{2\pi r}{2\pi}$$

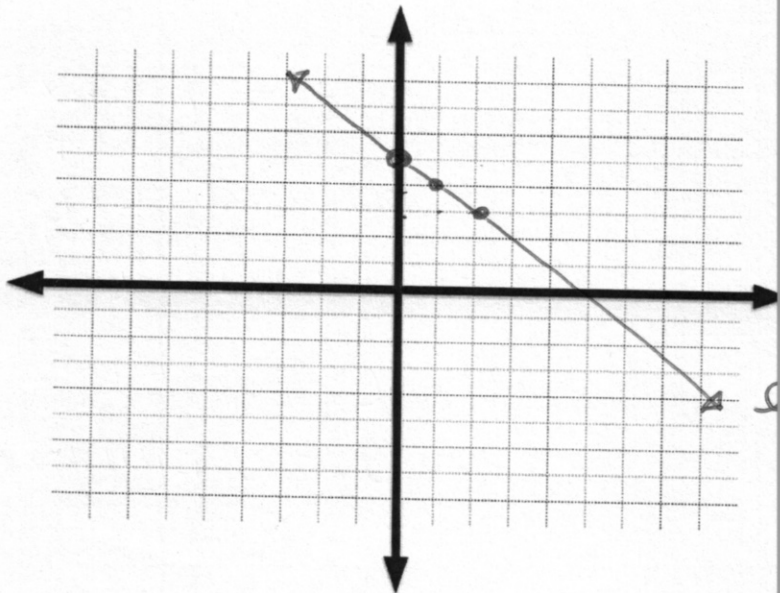
$$\frac{C}{2\pi} = r \quad ; \quad \boxed{r = \frac{C}{2\pi}}$$

✓

33 ✓

Graph the following linear equations

3) $x + y = 5$

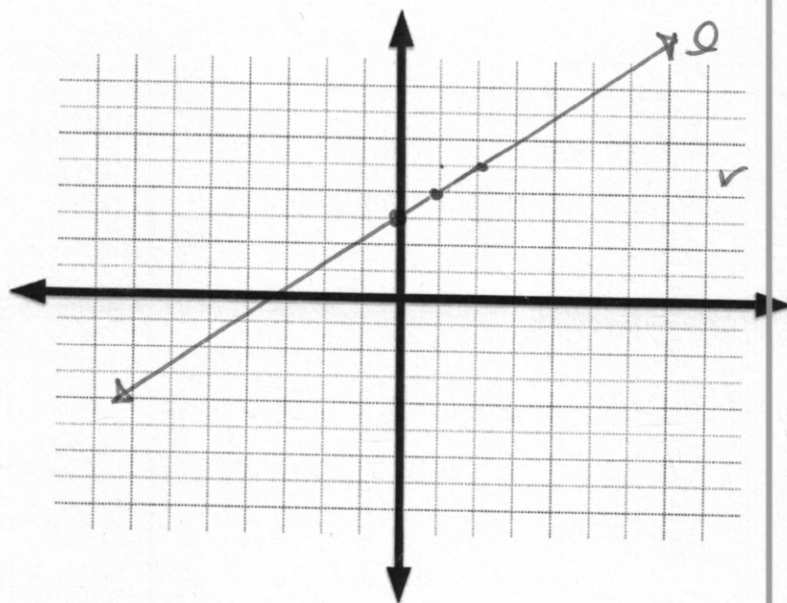


$$\begin{aligned} x + y &= 5 \\ -x &\quad -x \\ y &= -x + 5 \\ m &= -1 \quad ; \quad b = 5 \end{aligned}$$

✓ ✓

Sr

4) $x - y = -3$



$$\begin{array}{rcl} x - y & = & -3 \\ -x & & -x \end{array}$$

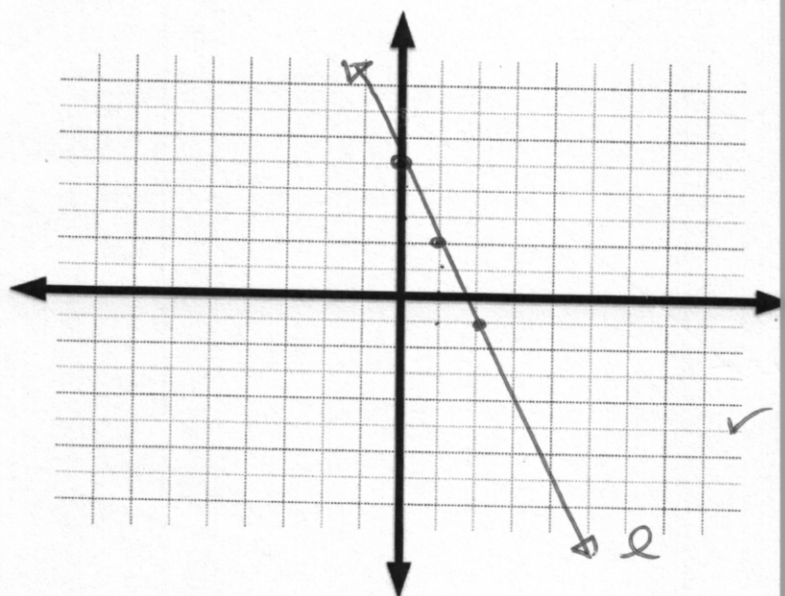
$$\frac{-y}{-1} = \frac{-x-3}{-1}$$

$$y = \frac{-x}{-1} - \frac{3}{-1}$$

$$y = x + 3$$

$$m = \frac{1}{1} ; b = 3$$

5) $3x + y = 5$



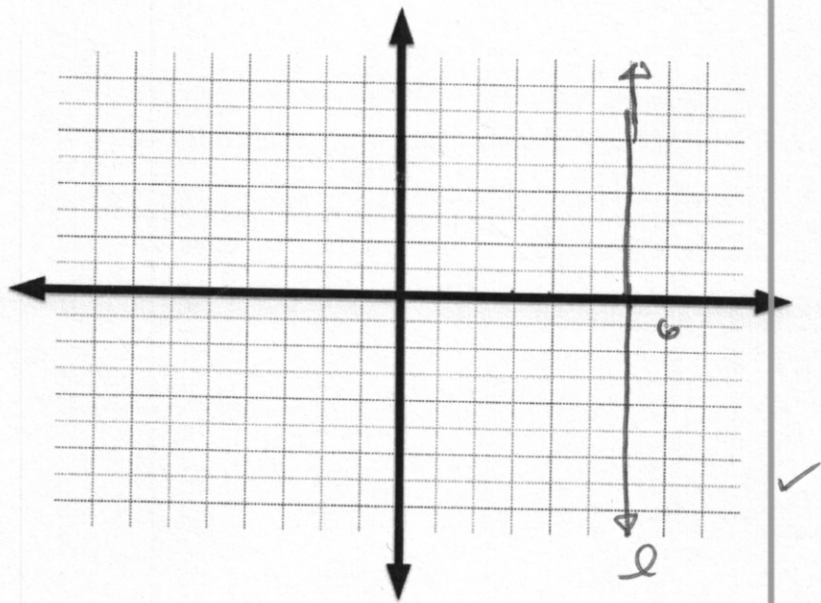
$$\begin{array}{rcl} 3x + y & = & 5 \\ -3x & & -3x \end{array}$$

$$y = -3x + 5$$

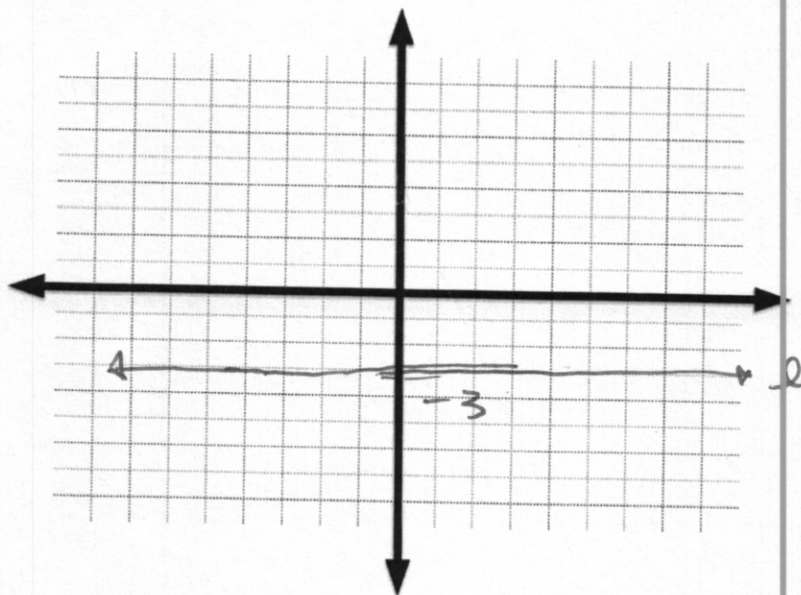
$$m = -\frac{3}{1} ; b = 5$$

6 ✓

6) $x = 6$



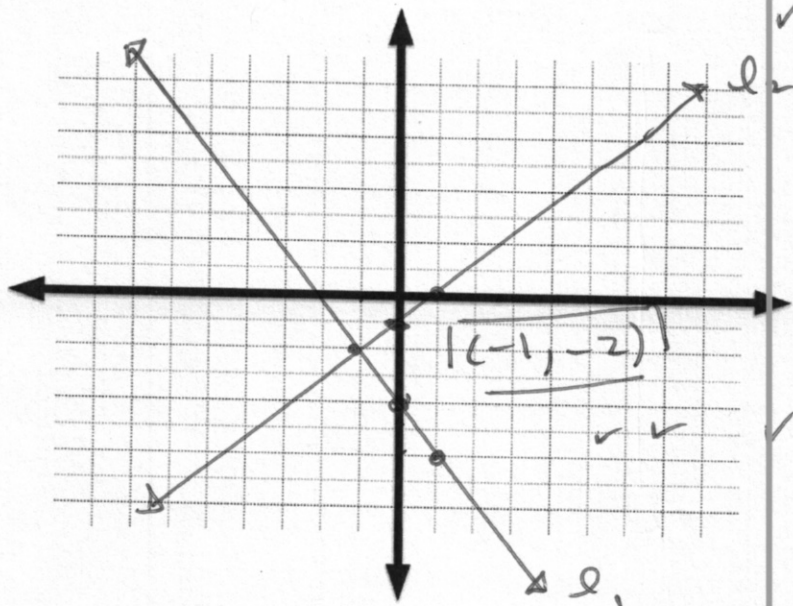
7) $y = -3$



8) Solve the linear system by graphing.

$$L_1 \quad 2x + y = -4$$

$$L_2 \quad x - y = 1$$



$$(L_1) \quad \begin{array}{rcl} 2x + y & = & -4 \\ -2x & & -2x \end{array}$$

$$y = -2x - 4$$

$$m = -\frac{2}{1} ; b = -4$$

$$(L_2) \quad \begin{array}{rcl} x - y & = & 1 \\ -x & & -x \end{array}$$

$$\frac{-y}{-1} = \frac{-x + 1}{-1}$$

$$y = \frac{-x}{-1} + \frac{1}{-1}$$

$$y = x - 1$$

$$m = 1 ; b = -1$$

Determine the equation of the line that:

9) Passes through the point $(1, -3)$ with slope of 4

$$y - y_1 = m(x - x_1)$$

$$y - (-3) = 4(x - 1)$$

$$y + 3 = 4x - 4$$

10) Passes through the points $(0, -5)$ and $(2, -1)$

$$y - y_1 = m(x - x_1)$$

$$y - (-5) = 2(x - 0)$$

$$y + 5 = 2x$$

$$y = 2x - 5$$

$$y = 4x - 7$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{-1 - (-5)}{2 - 0}$$

$$m = \frac{-1 + 5}{2}$$

$$m = \frac{4}{2}$$

$$m = 2$$

8 ✓

- 11) Passes through the point $(0,6)$ and is parallel to the equation $x + y = -3$

$$y - y_1 = m(x - x_1)$$

$$y - 6 = -1(x - 0)$$

$$\begin{array}{r} y - 6 = -x \\ +6 \quad +6 \end{array}$$

$$\boxed{y = -x + 6} \quad \checkmark \checkmark$$

$$\begin{array}{r} -x \quad -x \\ y = -x - 3 \end{array}$$

$$m_1 = m_2$$

$$b_1 \neq b_2$$

$\underline{l_1 \parallel l_2}$

- 12) Passes through the point $(1,2)$ and is perpendicular to the equation $x + 3y = -12$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 3(x - 1)$$

$$\begin{array}{r} y - 2 = 3x - 3 \\ +2 \quad +2 \end{array}$$

$$\boxed{y = 3x - 1} \quad \checkmark \checkmark$$

$\underline{l_1 \perp l_2}$

$$m_2 = -\frac{1}{3}$$

$$m_1 = 3$$

$$\begin{array}{r} -x \quad -x \\ 3y = -x - 12 \\ \frac{3y}{3} = \frac{-x - 12}{3} \end{array}$$

$$y = -\frac{1}{3}x - \frac{12}{3}$$

$$y = -\frac{1}{3}x - 4$$

- 13) Solve by the Graphical Method

$$\begin{array}{r} x - 2y = 2 \\ -x \quad -x \\ \hline -2y = -x + 2 \\ \hline -2 \quad -2 \end{array}$$

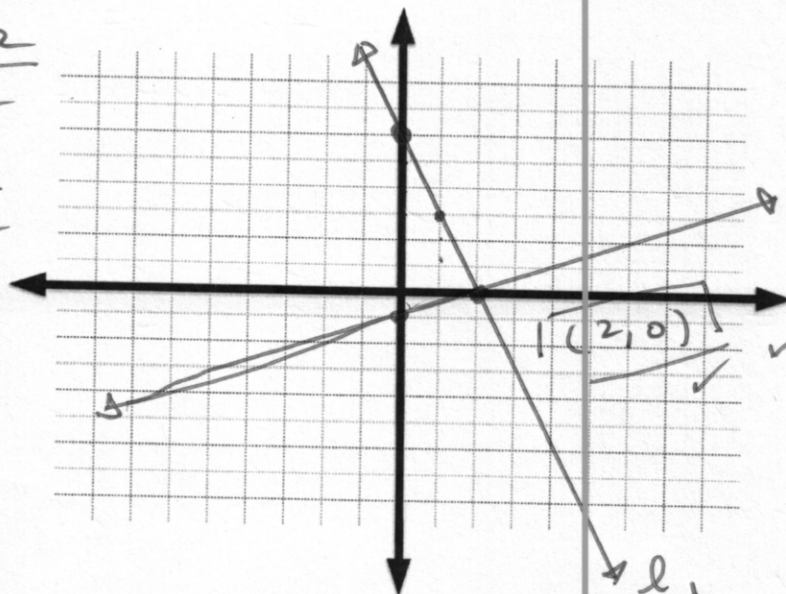
$$y = \frac{-x}{-2} + \frac{2}{-2}$$

$$y = \frac{1}{2}x - 1$$

$$\begin{array}{l} l_1: 3x + y = 6 \\ l_2: x - 2y = 2 \end{array}$$

$$(l_1) y = -3x + 6$$

$$(l_2) y = \frac{1}{2}x - 1$$



8✓

14) Solve the system by the Addition Method.

$$\begin{array}{l} \textcircled{e_1} \quad 2x + y = 7 \\ \textcircled{e_2} \quad -x + 3y = -7 \end{array}$$

$$\textcircled{e_1} \quad 2x + y = 7$$

$$\textcircled{e_2} \quad 2(-x + 3y) = -7 \cdot 2 \quad ; \quad \begin{array}{r} 2x + y = 7 \\ -2x + 6y = -14 \\ \hline 7y = -7 \end{array}$$

use back sub

$$\begin{array}{r} 2x + y = 7 \\ -1 \\ \hline 2x - 1 = 7 \end{array}$$

$$\begin{array}{r} 2x - 1 = 7 \\ +1 \quad +1 \\ \hline 2x = 8 \end{array}$$

$$\frac{2x}{2} = \frac{8}{2}$$

$$\frac{7y}{7} = \frac{-7}{7}$$

$$\therefore y = -1$$

$$\textcircled{x = 4}$$

$$\boxed{(4, -1)}$$

15) Solve by the Substitution Method

$$\begin{array}{l} \textcircled{e_1} \quad x + 3y = 4 \\ \textcircled{e_2} \quad 2x - 5y = 8 \end{array}$$

$$\begin{array}{r} x + 3y = 4 \\ -3y \quad -3y \\ \hline x = -3y + 4 \end{array}$$

$$\textcircled{e_1} \quad x = -3y + 4$$

Sub into $\textcircled{e_2}$

$$\begin{array}{r} 2x - 5y = 8 \\ \varnothing \\ -3y + 4 \end{array}$$

$$-3y + 4$$

$$2(-3y + 4) - 5y = 8$$

$$-6y + 8 - 5y = 8$$

$$\begin{array}{r} -11y + 8 = 8 \\ -8 \quad -8 \\ \hline -11y = 0 \end{array}$$

$$\frac{-11y}{-11} = \frac{0}{-11}$$

$$\textcircled{y = 0}$$

use back sub

$$\begin{array}{r} x = -3y + 4 \\ \varnothing \\ 0 \end{array}$$

4 ✓

$$x = -3 \cdot 0 + 4$$

$$x = 0 + 4$$

$$\textcircled{x = 4}$$

✓ ✓

$$\boxed{(4, 0)}$$