

# Implicit Differentiation

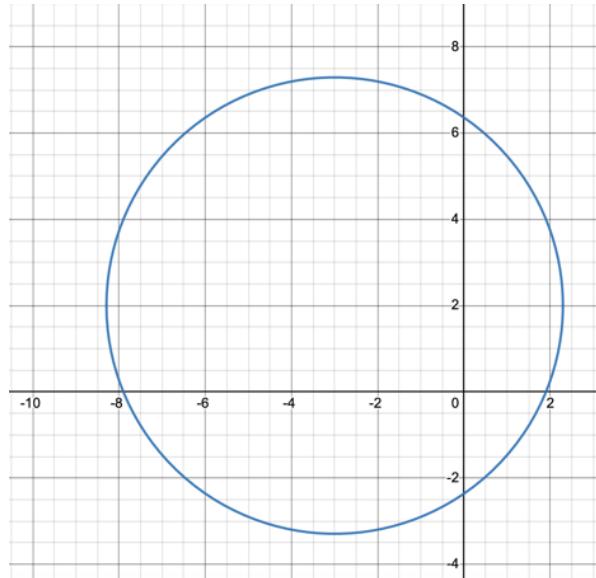
## Performing a Derivative on a Relation

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Determine  $\frac{dy}{dx}$ .

**Circle**

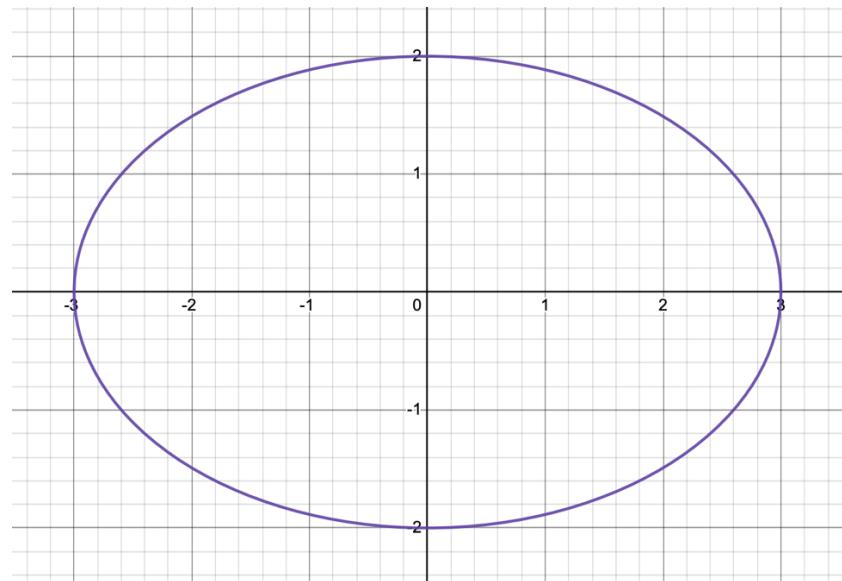
$$x^2 + y^2 + 6x - 4y = 15$$





**Ellipse**

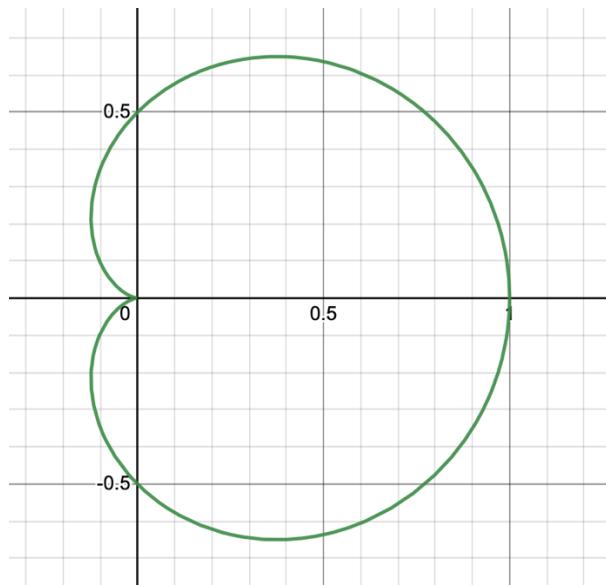
$$4x^2 + 9y^2 = 36$$





### Cardioid

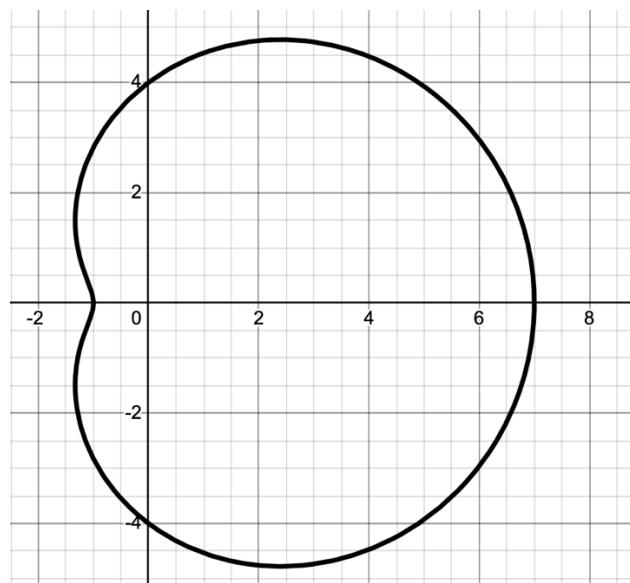
$$x^2 + y^2 = (2x^2 + 2y^2 - x)^2$$





**Limicon**

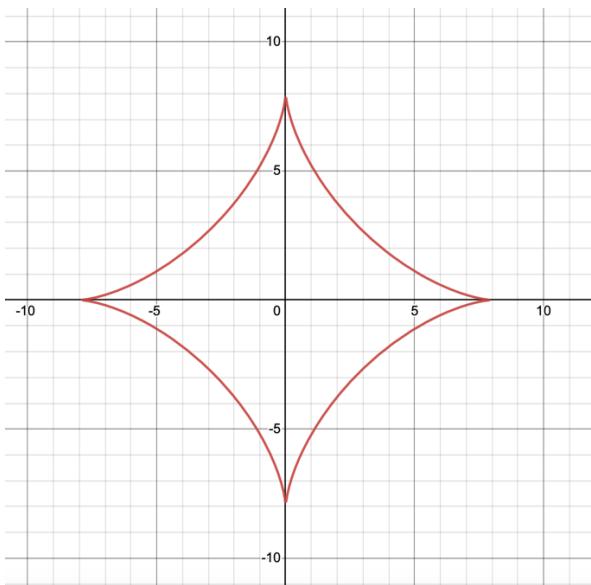
$$(x^2 + y^2 - 3x)^2 = 16(x^2 + y^2)$$





### Astroid

$$x^{2/3} + y^{2/3} = 4$$



## Lemniscate

$$(x^2 + y^2)^2 = 4(x^2 - y^2)$$

