

Graphing Sine and Cosine

$$y = a\sin(kx)$$

$$y = a\cos(kx)$$

$$k > 0$$

$$\text{Amp} = |a| \text{ and Period } p = \frac{2\pi}{k}$$

$$\text{Interval of One Cycle} = [0, p]$$

Determine the amplitude, period, interval of one cycle, x-intercepts, max value, min value, and use this information to sketch the curve.

1. $y = 3\sin(4x)$

2. $y = 2\sin(3x)$

3. $y = -\sin(\pi x)$

4. $y = -\sin(2\pi x)$

5. $y = \frac{1}{3}\cos(2\pi x)$

6. $y = \frac{2}{3}\cos(-\pi x)$

7. $y = 4\sin(2x)$

8. $y = 5\sin(3x)$

9. $y = 3\cos\left(\frac{x}{2}\right)$

10. $y = 5\cos\left(\frac{x}{3}\right)$

11. $y = -2\sin\left(\frac{x}{4}\right)$

12. $y = -3\sin\left(\frac{x}{2}\right)$

13. $y = -\cos\left(\frac{x}{2}\right)$

14. $y = 5\cos\left(\frac{x}{4}\right)$

15. $y = \sin(4x)$

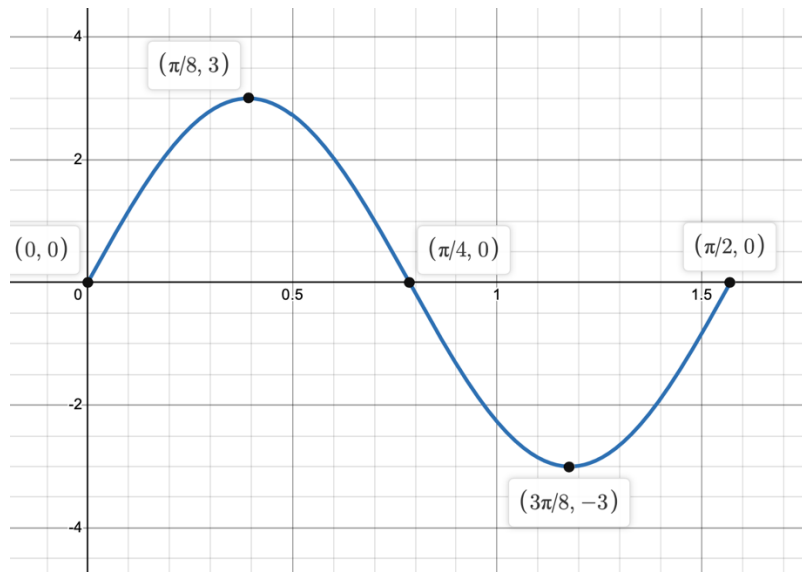
16. $y = \sin(6\pi x)$

17. $y = \cos(3\pi x)$

18. $y = \frac{5}{2}\cos(-4x)$

Answers

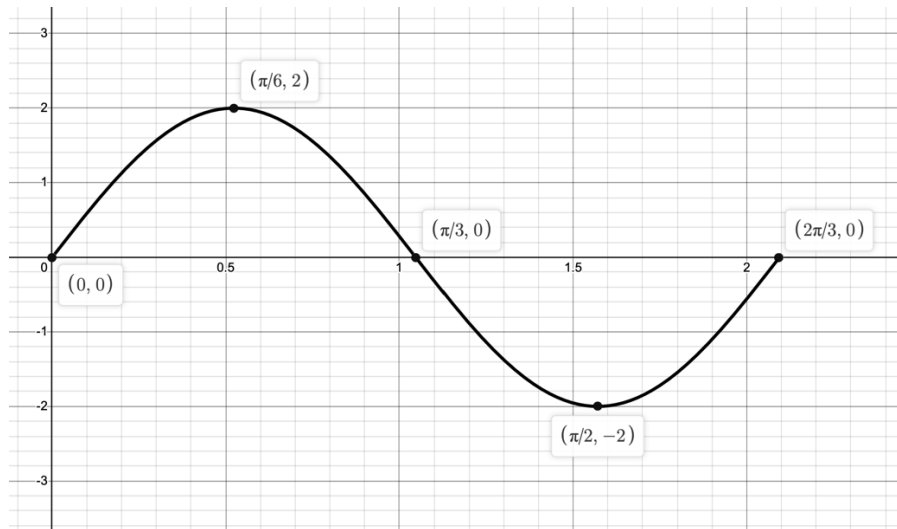
1.



$$\text{amp} = 3, \text{period} = \frac{\pi}{2}, \text{Interval} = \left[0, \frac{\pi}{2}\right], \text{xint: } x = 0, x = \frac{\pi}{4}, x = \frac{\pi}{2}$$

$$\text{min} = -3, \text{max} = 3$$

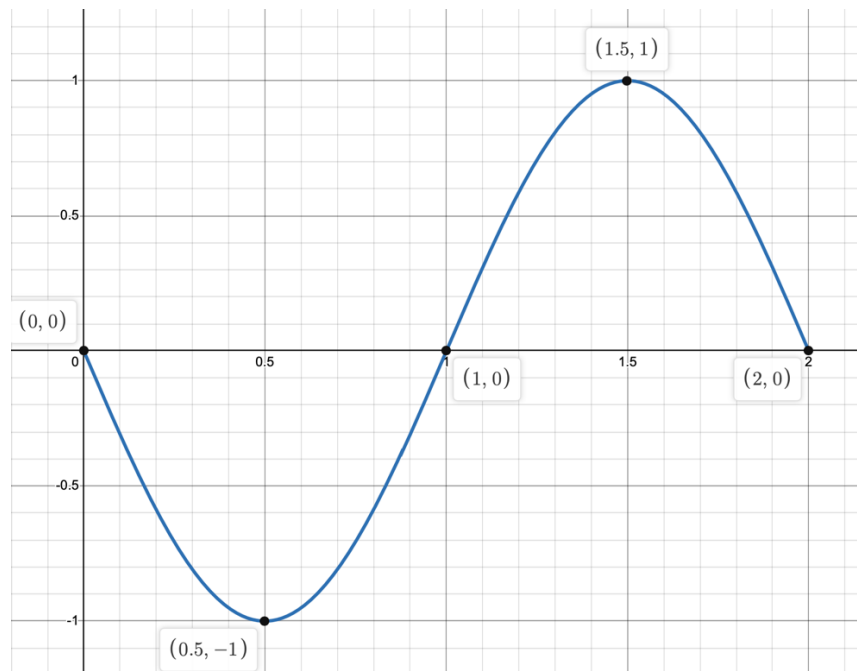
2.



$$\text{amp} = 2, \text{period} = \frac{2\pi}{3}, \text{Interval} = \left[0, \frac{2\pi}{3}\right], \text{xint: } x = 0, x = \frac{\pi}{3}, x = \frac{2\pi}{3}$$

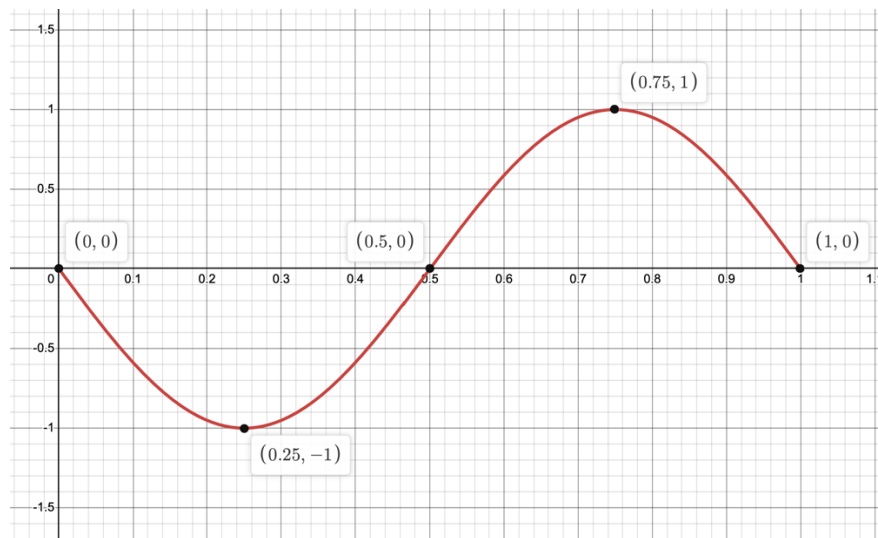
$$\text{min} = -2, \text{max} = 2$$

3.



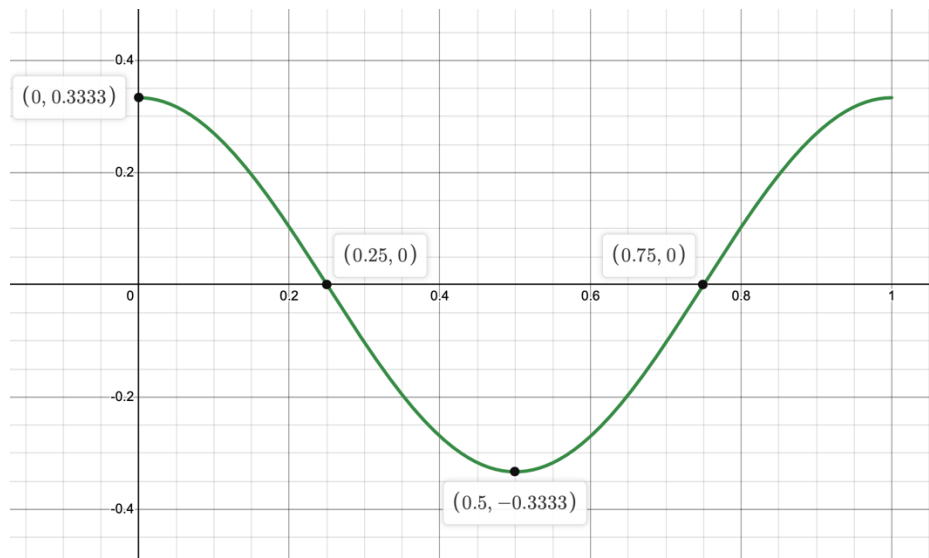
$amp = 1, period = 2, Interval = [0, 2], xint: x = 0, x = 1, x = 2$
 $min = -1, max = 1$

4.



$amp = 1, period = 1, Interval = [0, 1], xint: x = 0, x = \frac{1}{2}, x = 1$
 $min = -1, max = 1$

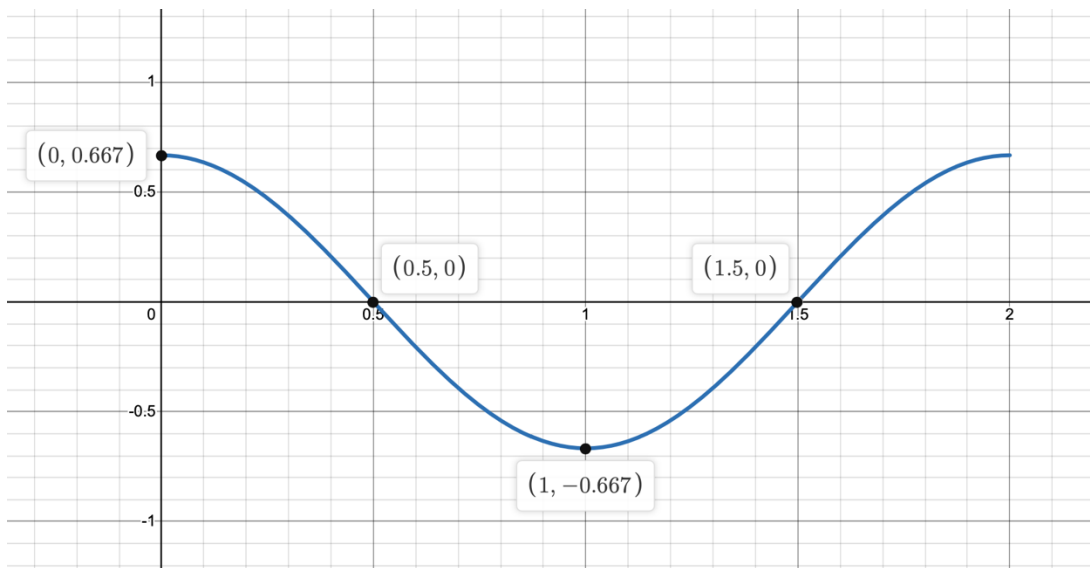
5.



$$\text{amp} = \frac{1}{3}, \text{period} = 1, \text{Interval} = [0, 1], \text{xint: } x = \frac{1}{4}, x = \frac{3}{4}$$

$$\text{min} = -\frac{1}{3}, \text{max} = \frac{1}{3}$$

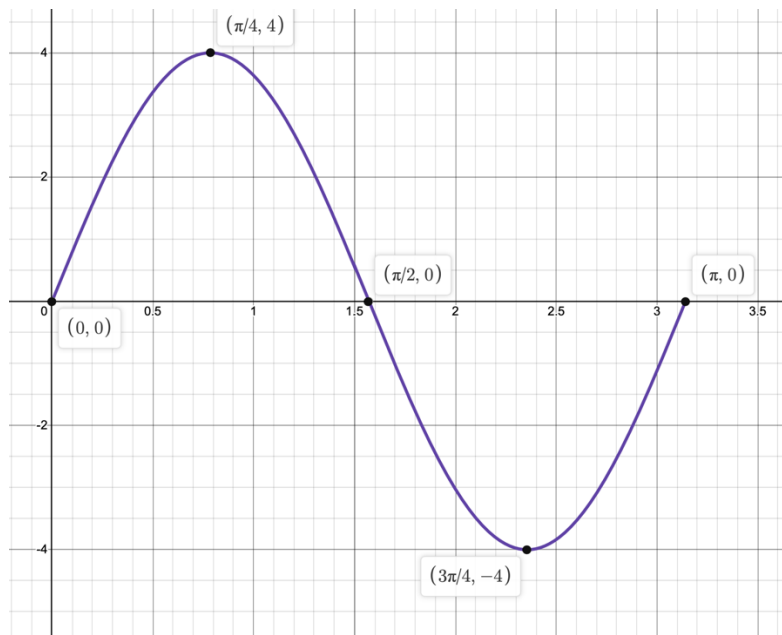
6.



$$\text{amp} = \frac{2}{3}, \text{period} = 2, \text{Interval} = [0, 2], \text{xint: } x = \frac{1}{2}, x = \frac{3}{2}$$

$$\text{min} = -\frac{2}{3}, \text{max} = \frac{2}{3}$$

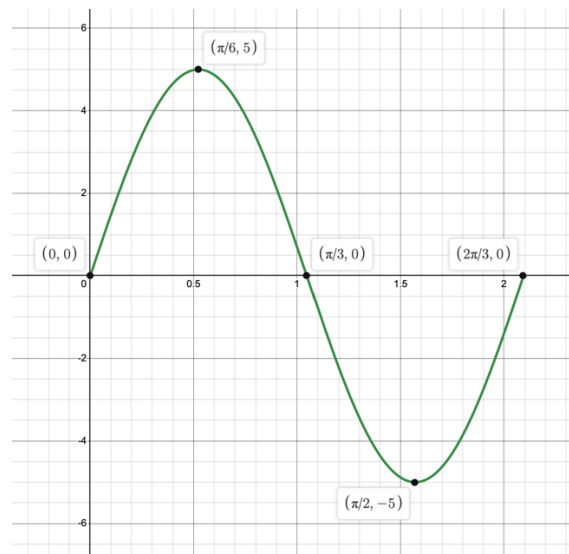
7.



$$\text{amp} = 4, \text{period} = \pi, \text{Interval} = [0, \pi], \text{xint: } x = 0, x = \frac{\pi}{2}, x = \pi$$

$$\text{min} = -4, \text{max} = 4$$

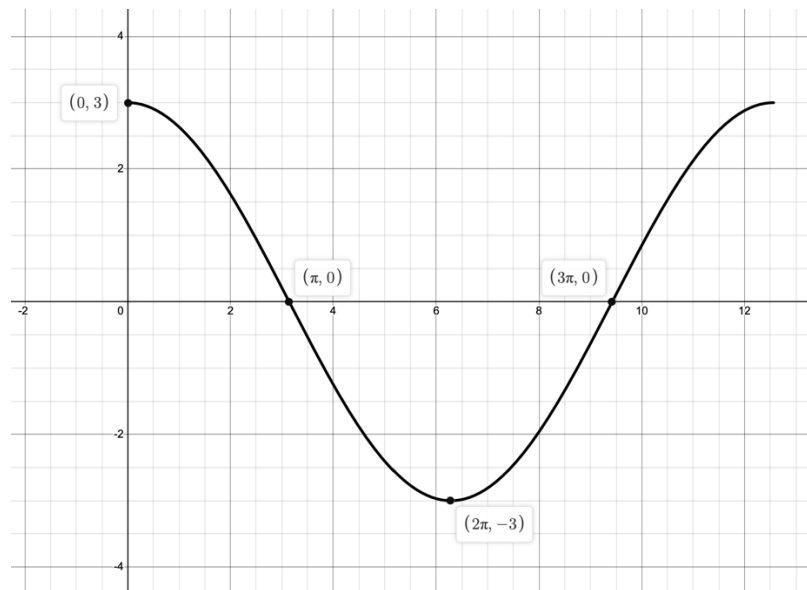
8.



$$\text{amp} = 5, \text{period} = \frac{2\pi}{3}, \text{Interval} = \left[0, \frac{2\pi}{3}\right], \text{xint: } x = 0, x = \frac{\pi}{3}, x = \frac{2\pi}{3}$$

$$\text{min} = -5, \text{max} = 5$$

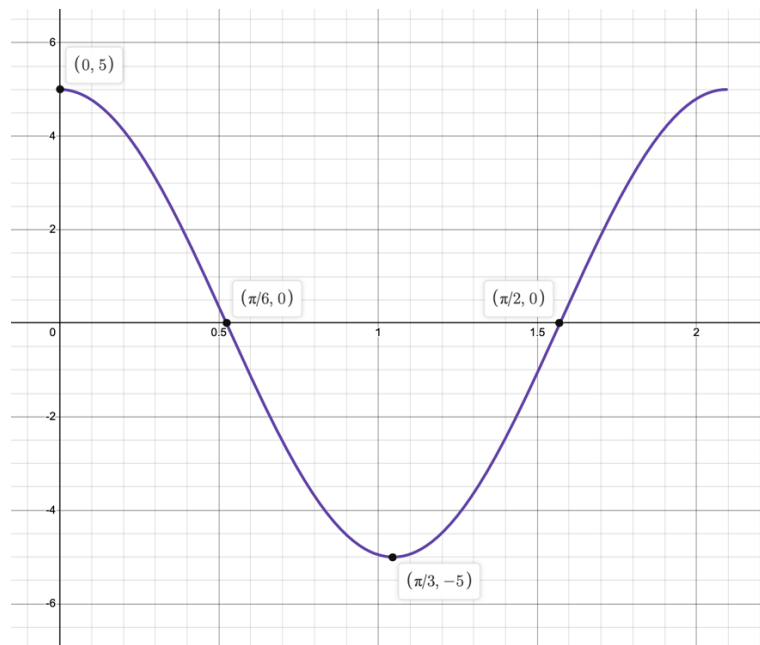
9.



$$\text{amp} = 3, \text{period} = 4\pi, \text{Interval} = [0, 4\pi], \text{xint: } x = \pi, x = 3\pi$$

$$\text{min} = -3, \text{max} = 3$$

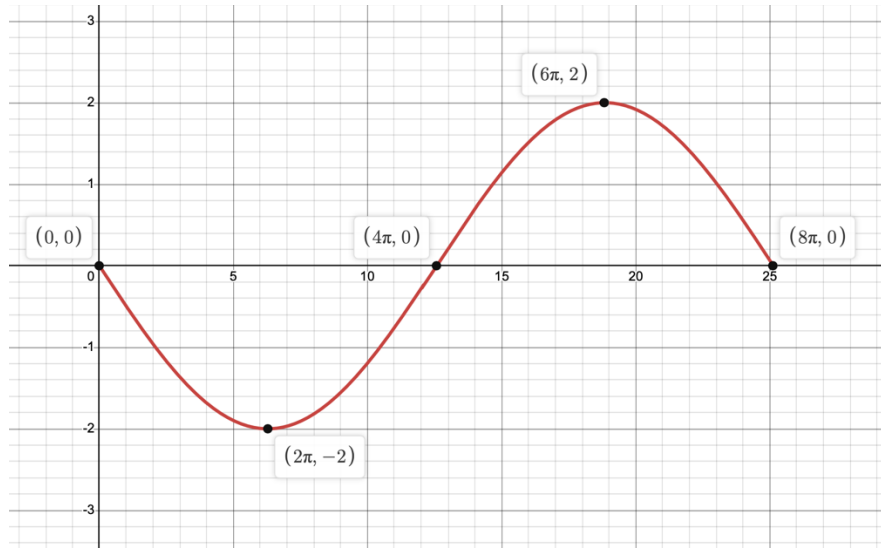
10.



$$\text{amp} = 5, \text{period} = \frac{2\pi}{3}, \text{Interval} = \left[0, \frac{2\pi}{3}\right], \text{xint: } x = \frac{\pi}{6}, x = \frac{\pi}{2}$$

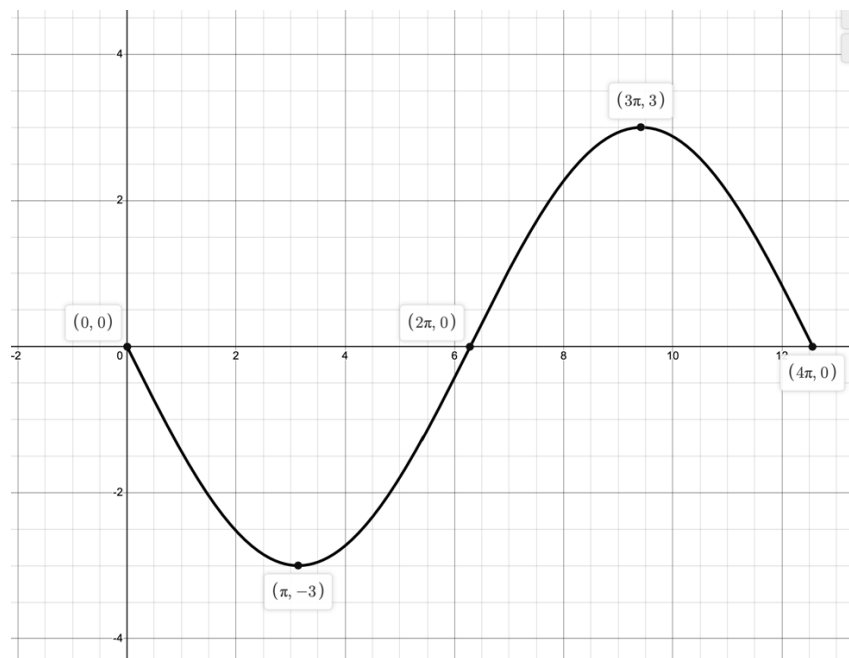
$$\text{min} = -5, \text{max} = 5$$

11.



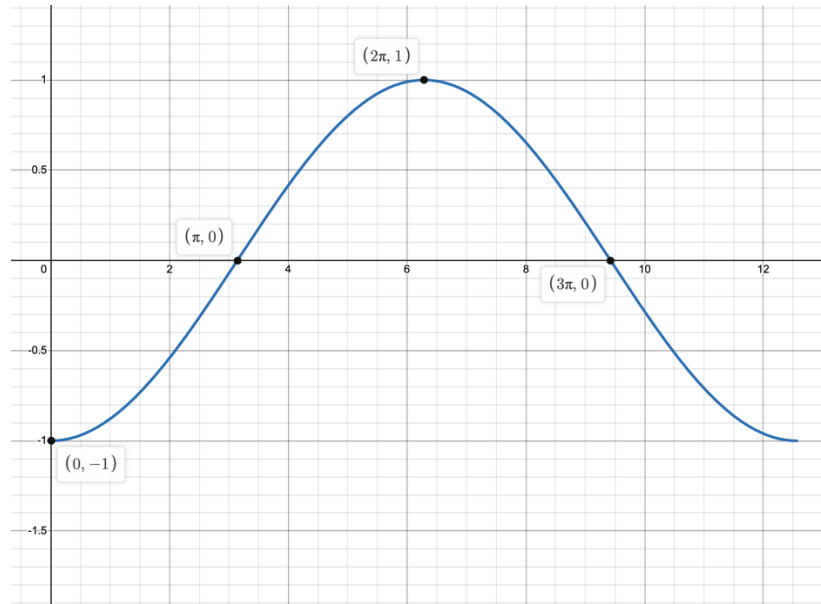
$amp = 2, period = 8\pi, Interval = [0, 8\pi], x_{int}: x = 0, x = 4\pi, x = 8\pi$
 $min = -2, max = 2$

12.



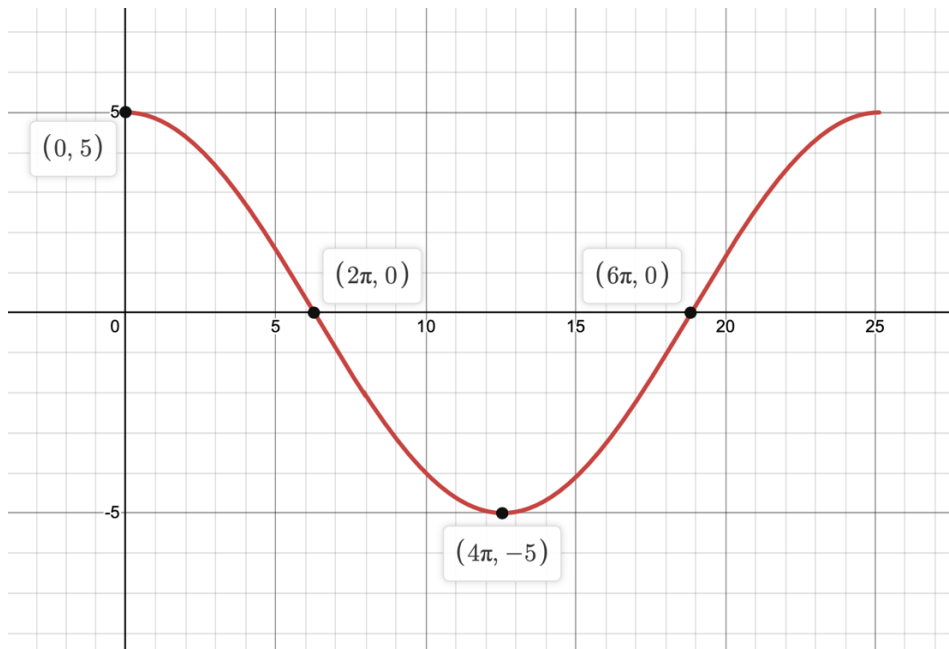
$amp = 3, period = 4\pi, Interval = [0, 4\pi], x_{int}: x = 0, x = 2\pi, x = 4\pi$
 $min = -3, max = 3$

13.



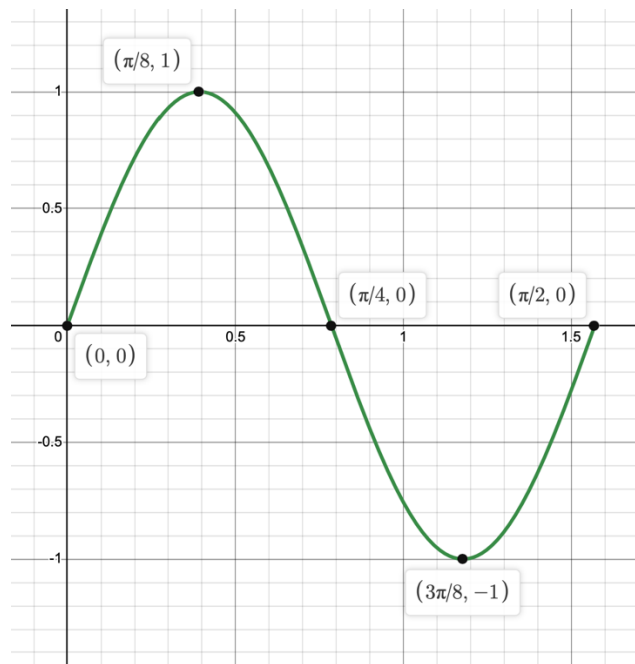
$amp = 1, period = 4\pi, Interval = [0, 4\pi], xint: x = \pi, x = 3\pi$
 $min = -1, max = 1$

14.



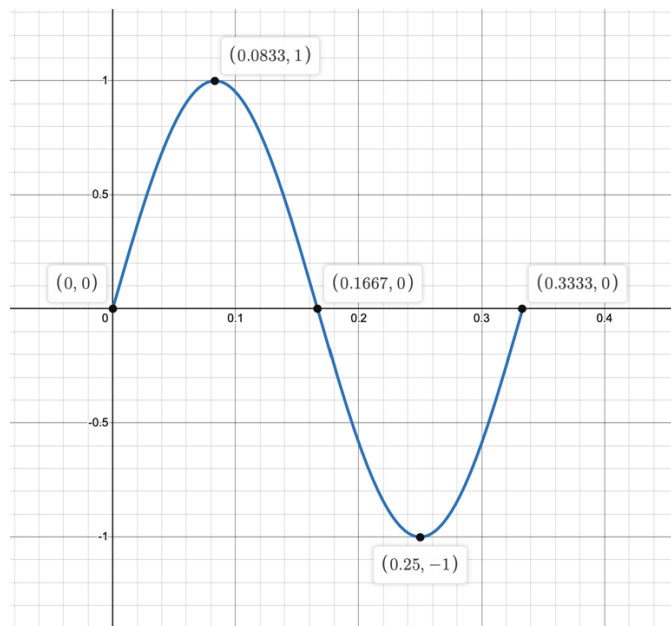
$amp = 5, period = 8\pi, Interval = [0, 8\pi], xint: x = 2\pi, x = 6\pi$
 $min = -5, max = 5$

15.



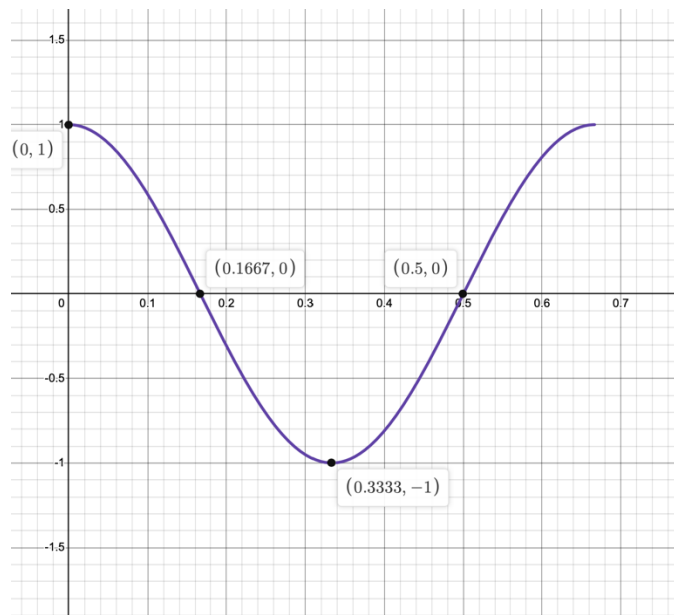
$$\begin{aligned} \text{amp} &= 1, \text{period} = \frac{\pi}{2}, \text{Interval} = \left[0, \frac{\pi}{2}\right], x_{\text{int}}: x = 0, x = \frac{\pi}{4}, x = \frac{\pi}{2} \\ \text{min} &= -1, \text{max} = 1 \end{aligned}$$

16.



$$\begin{aligned} \text{amp} &= 1, \text{period} = \frac{1}{3}, \text{Interval} = \left[0, \frac{1}{3}\right], x_{\text{int}}: x = 0, x = \frac{1}{6}, x = \frac{1}{3} \\ \text{min} &= -1, \text{max} = 1 \end{aligned}$$

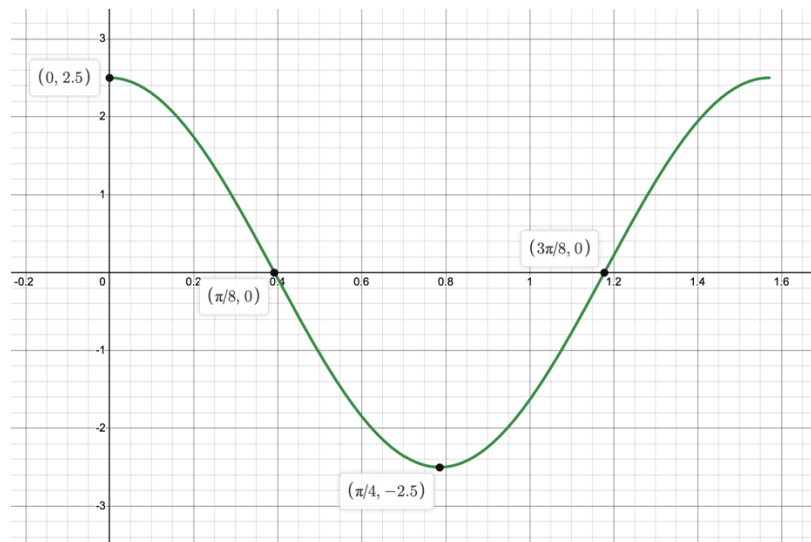
17.



$$\text{amp} = 1, \text{period} = \frac{2}{3}, \text{Interval} = \left[0, \frac{2}{3}\right], \text{xint: } x = \frac{1}{6}, x = \frac{1}{2}$$

$$\text{min} = -1, \text{max} = 1$$

18.



$$\text{amp} = \frac{5}{2}, \text{period} = \frac{\pi}{2}, \text{Interval} = \left[0, \frac{\pi}{2}\right], \text{xint: } x = \frac{\pi}{8}, x = \frac{3\pi}{8}$$

$$\text{min} = -\frac{5}{2}, \text{max} = \frac{5}{2}$$