East Los Angeles College Department of Mathematics Math 241 Final Exam Study Guide

An airplane flies at a speed of 300 mph in a heading N30W. The wind is traveling at a speed of 20 mph in a heading due South.

- 1. Determine the velocity vector of the airplane.
- 2. Determine the velocity vector of the wind.
- 3. Determine the resultant vector.
- 4. Determine the airplanes true speed with the wind.
- 5. Determine the airplanes true heading.

Forces on an object.

Let
$$\overline{F_1} = -8i + 3j$$
 and $\overline{F_2} = 4i - 2j$ and $\overline{F_3} = i + j$

- 6. Determine the resultant force vector.
- 7. Determine the magnitude of the resultant force vector.
- 8. Determine the standard angle (direction) of the resultant force vector.

Let $r = 3 + 3sin(\theta)$

9. Determine the Cartesian coordinate equation.

10. Graph $y = 3 + 3sin(\theta)$ over $0 \le \theta \le 2\pi$

11. Graph the polar equation $r = 3 + 3sin(\theta)$.

Let $r^2 = cos(2\theta)$ 12. Determine the Cartesian coordinate equation.

13. Graph $y = cos(2\theta)$ over $0 \le \theta \le 2\pi$

14. Graph the polar equation $r^2 = cos(2\theta)$

Solve the following trigonometric equations for θ over $0 \le \theta \le 2\pi$ 15. $\cot(2\theta) = -1$ 16. $\sqrt{2}\cos\left(\frac{\theta}{2}\right) - 1 = 0$ 17. $(2\sin(\theta) + 1)(\tan(\theta) - 1) = 0$ 18. $2\sin^2(3\theta) = 1$

Navigation

19. Two boats leave the same port at the same time. One travels at a speed of 45 mph in the direction N60E and the other travels at the speed of 65 mph in a direction S20E. After 2 hours, how far apart are the boats?



Determine the following values.

- 20. Angle C
- 21. *AC*
- 22. *BC*



Determine the following values.

23. Angle B

24. Angle C 25. *BC*

26. Determine the area of the shaded region.



Speed of a Car

27. The wheels of a car have a radius of 12 inches and are rotating at 500 rpm. Determine the speed of a car in mph.

Truck wheels

A truck with 46-inch diameter wheels is traveling at 60 mph.

28. Determine the angular speed of the wheels in radians per minute.

29. How many rpm's do the wheels make?

$$y = tan\left(2\left(x + \frac{\pi}{4}\right)\right)$$

30. Determine the period.

- 31. Determine the phase shift.
- 32. Determine the interval of one cycle.
- 33. Graph the curve.

$$y = \cot\left(\frac{1}{4}\left(x - \frac{\pi}{3}\right)\right)$$

- 34. Determine the period.
- 35. Determine the phase shift.
- 36. Determine the interval of one cycle.
- 37. Graph the curve.