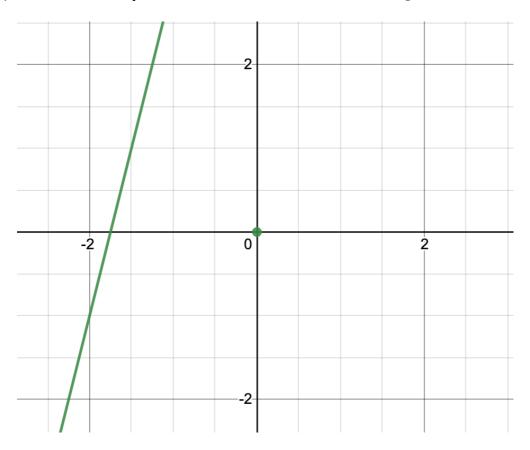
### **Optimization**

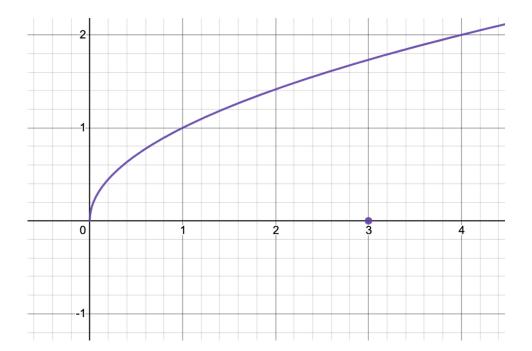
Application of finding extreme values (Minimum or Maximum) for a function.

Example 1

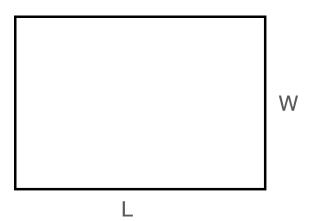
Find a point on the line y = 4x + 7 that is closest to the origin (0,0).



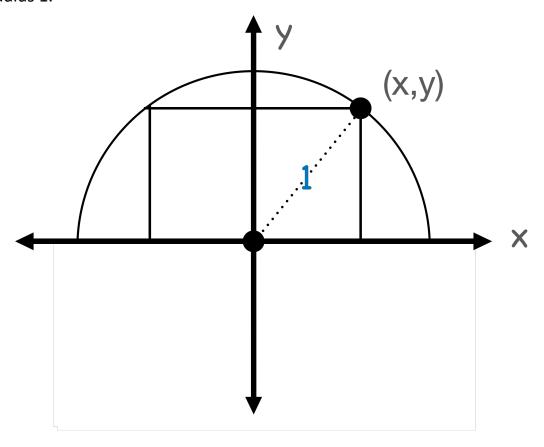
Find the point on the curve  $y = \sqrt{x}$  that is closest to (3,0).



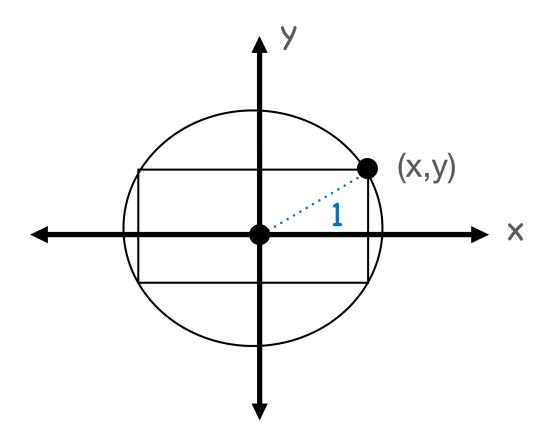
A farmer has 500 feet of fence that enclose a rectangular area. What dimensions maximize the area?



Find the dimensions of the largest rectangle that can be inscribed in a semi-circle of radius 1.

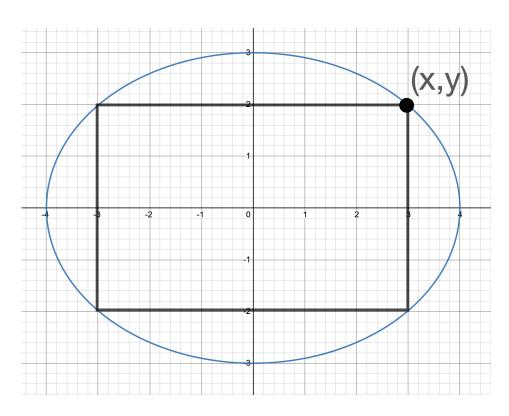


**Example 5** Find the dimensions of the largest rectangle that can be inscribed in a unit circle.



Find the area of the largest rectangle that can be inscribed in the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$ 

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$



A boat leaves a dock at 2:00 PM and travels due South at a speed of 20 km/h. Another boat has been heading due East at 15 km/h and reaches the same dock at 3:00 PM. At what time t where the two boats closest together?

